

Introduction

“What is the optimal portfolio?” A question that has been discussed and debated since Harry Markowitz introduced modern portfolio theory (MPT) in his 1952 essay “Portfolio Selection.” While practitioners continue to look for ways to improve upon MPT, the underlying concept of the efficient frontier remains a cornerstone in portfolio theory. By using MPT, we can compare different portfolio configurations and see how adjusting for return and risk changes the allocation to each fund.

“Art and science encounter each other when they seek exactitude.”

– Étienne-Jules Marey

Methodology

Prior to diving into our methodology, a number of assumptions and limitations to the process are worth highlighting.

Sample Size – For purposes of this exercise, we chose 8 funds that are well-known to Silver Creek. The time series for each of the 8 funds differs in length with the longest data set starting in 2004 and the shortest data set starting in 2010. In order to be uniform across time series, we decided to start all of the funds’ data sets in 2010. While this is a relatively small sample size for each fund of just over 60 data points, we felt it best to standardize the time series for the sake of comparison. However, it is worth noting that a larger sample size may deliver materially different results including the potential for a non-normal distribution.

Normal Distribution – A basic assumption of MPT is that returns follow a normal distribution. Of the 8 funds selected, 5 exhibited relatively normal return distributions and 3 demonstrated non-normal distributions. For research and consistency purposes, we assumed a normal distribution given that 5 of the 8 funds displayed this characteristic.

Historical Data – The underlying concept of MPT is to maximize expected return for a given level of risk. However, in practice,

predictions are based on historical data, which does not take into account environments that did not exist. Given that it is impossible to predict the future, we must consider other factors when constructing a portfolio. For example, we may increase the allocation to a manager with whom we have experience as we have more confidence in their ability to meet their expected return. On the other hand, we may look to grow with a newer manager in order to build our conviction.

Other Factors – In the context of a broad portfolio, we must also consider the role a fund plays, as well as how the fund performs in various market conditions. For example, although a fund’s return expectations are at the lower end of the spectrum, it may show minimal correlation to any of the other funds in the portfolio. As another example, we could allocate to a fund or strategy if it has proven to be uncorrelated in specific markets. For example, CTAs, at times, have performed well during crises. Although there is no guarantee that this strategy will generate returns in these environments, it may be prudent to have an allocation to CTAs as potential protection in difficult markets.

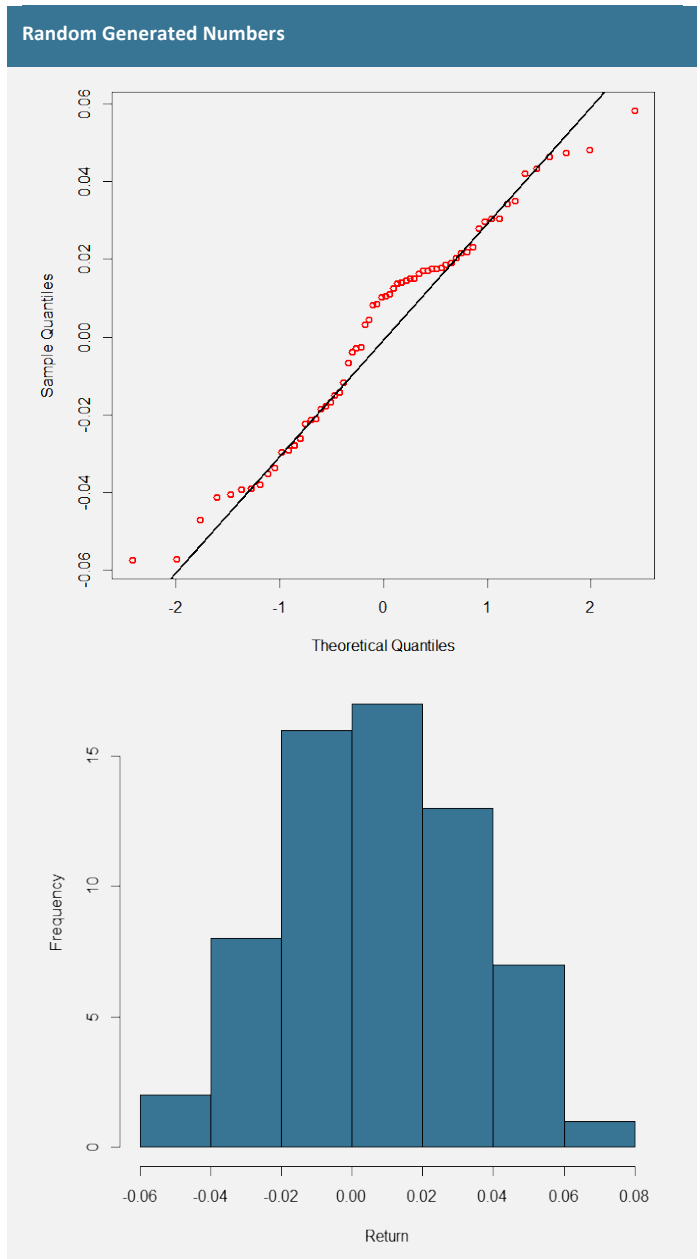
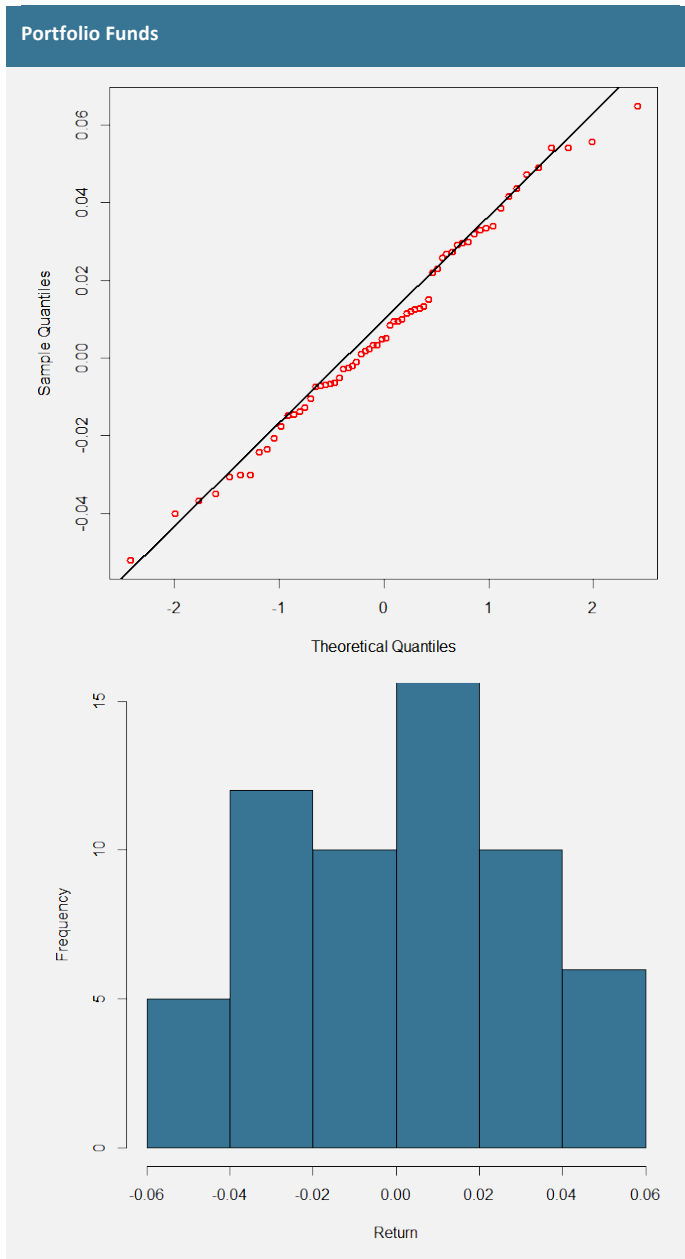
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As noted above, one of the major criticisms of MPT is that the theory assumes a normal distribution. In order to see if the 8-fund portfolio satisfied this assumption, we analyzed each of the funds. For reference, the QQ plot (a plot of quantiles of the first data set against the quantiles of the second data set) and return distribution of one of the funds is shown below.



Overall, the QQ plot of the funds fits the normal distribution of the QQ line well with only a few outliers compared to the plot of random generated numbers. Although there is some skewness to the right of the return distribution, the funds' returns generally resemble a normal distribution. Given that 5 of the 8 funds exhibited a similar distribution, we decided to assume a normal distribution for research purposes. While we understand that this has limitations, we felt it best to be consistent across all 8 funds, particularly given that more than half displayed this characteristic.

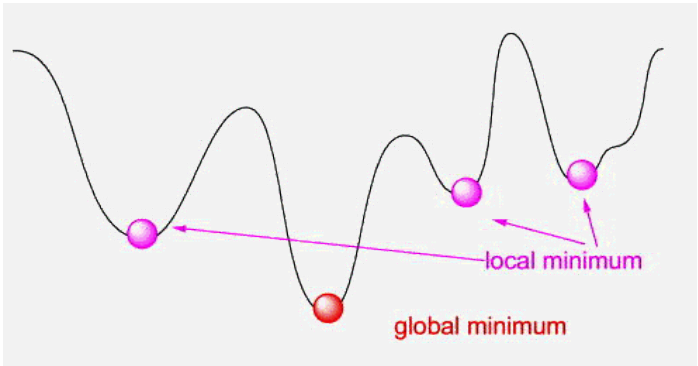
Mathematically, there are multiple ways to construct the optimization process with the most popular being non-linear programming, which comes with a utility function to describe the objective of the optimization and constraints. By taking the standard mean-variance portfolio optimization, the formula can be represented as follows:

$$\text{Maximize } r^T * w - \lambda * w^T * \Sigma * w$$

$$\text{subject to: } l_a \leq A * w \leq u_a$$

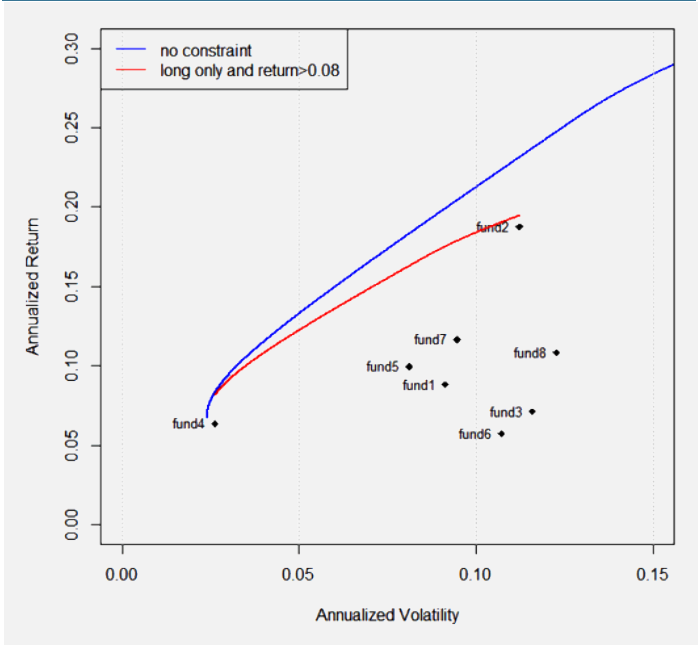
r = return vector
w = portfolio weight
Σ = covariance matrix
A = coefficient matrix for linear constraints
λ = coefficient of risk aversion

An optimal portfolio can be built to satisfy different return appetites and risk aversions. However, an unconstrained efficient frontier is of limited use as there are other factors to consider as previously discussed. In addition, the unconstrained efficient frontier can utilize short positions if it is determined to be necessary for an optimal portfolio. Given that it is impossible to short a fund, we must build in constraints to the efficient frontier. In this graph, we compare the unconstrained efficient frontier to a constrained efficient frontier, which only takes long positions and requires a portfolio return above 8%.



Given the differences in efficient frontiers, this analysis must be overlaid with the portfolio’s investment objectives. While it is convenient to build an optimized portfolio based solely on risk-return objectives, other scenarios must also be considered, which may not be linear combinations of return and risk. For example, maximum Sharpe Ratio or minimum expected tail risk should be analyzed. However, as these are non-linear, these scenarios can be optimized using the extrema among portfolios on the efficient frontier or other utility functions. One of the potential pitfalls in optimizations is that the process can return a local minimum (i.e. a point where the function value is smaller than at nearby points, but possibly greater than at a distant point in the search space).

Unconstrained Efficient Frontier vs. Constrained Efficient Frontier



In order to ensure that our optimization process captures the actual optimal portfolios, we cross validate the different scenarios.

Process

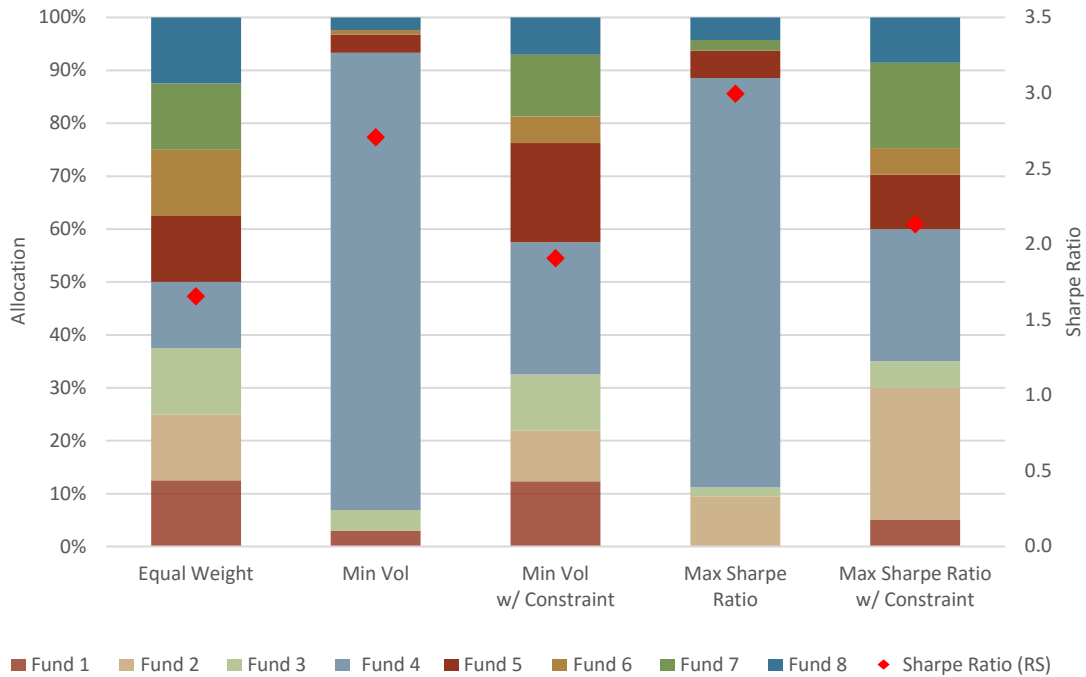
The funds chosen for this exercise are highly diversified with hundreds, and perhaps even thousands of underlying positions, which allows managers to construct portfolios with minimal correlation to broad markets. While this is compelling, it does not account for a fund’s correlation to factor exposures (e.g. momentum, value, quality), which can appear in funds from time to time. As it is difficult to know when this could occur, the risk can be mitigated through diversification across 8 funds with low pairwise correlation.

	Fund 1	Fund 2	Fund 3	Fund 4	Fund 5	Fund 6	Fund 7	Fund 8
Fund 1	1.0							
Fund 2	0.4	1.0						
Fund 3	0.3	0.3	1.0					
Fund 4	0.0	0.1	-0.1	1.0				
Fund 5	0.6	0.3	0.2	0.0	1.0			
Fund 6	0.5	0.3	0.3	-0.1	0.7	1.0		
Fund 7	0.3	0.3	0.3	0.1	0.5	0.4	1.0	
Fund 8	0.2	0.1	0.3	-0.1	0.4	0.5	0.3	1.0

In order to help determine the allocation to each fund, we analyzed 5 scenarios including:

- Equal Weight
- Minimum Volatility
- Minimum Volatility with Constraint
- Maximum Sharpe Ratio
- Maximum Sharpe Ratio with Constraint

The constraint used was that each fund allocation must be greater than 5%, but less than 25% of the portfolio.



	Equal Weight	Min Vol	Min Vol w/ Constraint	Max Sharpe Ratio	Max Sharpe Ratio w/ Constraint
Return	10.2%	6.8%	9.9%	8.2%	11.7%
Vol	6.0%	2.4%	5.1%	2.6%	5.3%
Sharpe Ratio	1.7	2.7	1.9	3.0	2.1

Equal Weight - While Equal Weight is the simplest with arguably the least overfitting, it also resulted in the lowest Sharpe Ratio as the annualized volatility was the highest of the 5 scenarios.

Minimum Volatility - Based on the historical return for each of the 8 funds, this scenario was designed to generate the lowest annualized volatility. Although the Sharpe Ratio was high, the annualized return was the lowest relative to the other scenarios. In addition, the scenario significantly over-weighted Fund 4, which had the lowest annualized volatility.

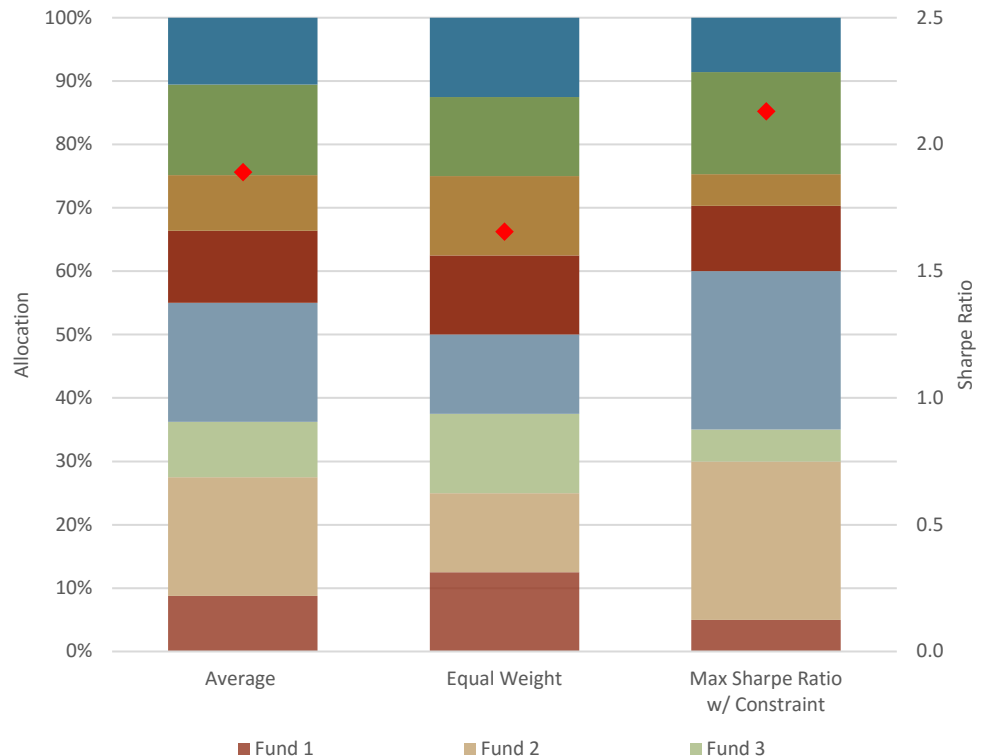
Minimum Volatility with Constraint - By constraining the scenario, the annualized volatility doubled, which resulted in a lower Sharpe Ratio as the annualized return did not increase proportionally to the increase in risk. While Fund 4 was still oversized, the allocation to each of the remaining funds was more balanced.

Maximum Sharpe Ratio - This scenario was constructed to produce the highest Sharpe Ratio using historical returns for each of the 8 funds. Similar to Minimum Volatility, Fund 4 was by far the largest allocation as it had the highest historical Sharpe Ratio.

Maximum Sharpe Ratio with Constraint - While constraints were used, this scenario resulted in the highest annualized return, as well as the highest Sharpe Ratio relative to the other constrained scenarios (i.e. Equal Weight and Minimum Volatility with Constraint). Allocations were reasonably balanced though there was still some concentration risk with the top 4 fund allocations totaling 76% of the portfolio.

Conclusion

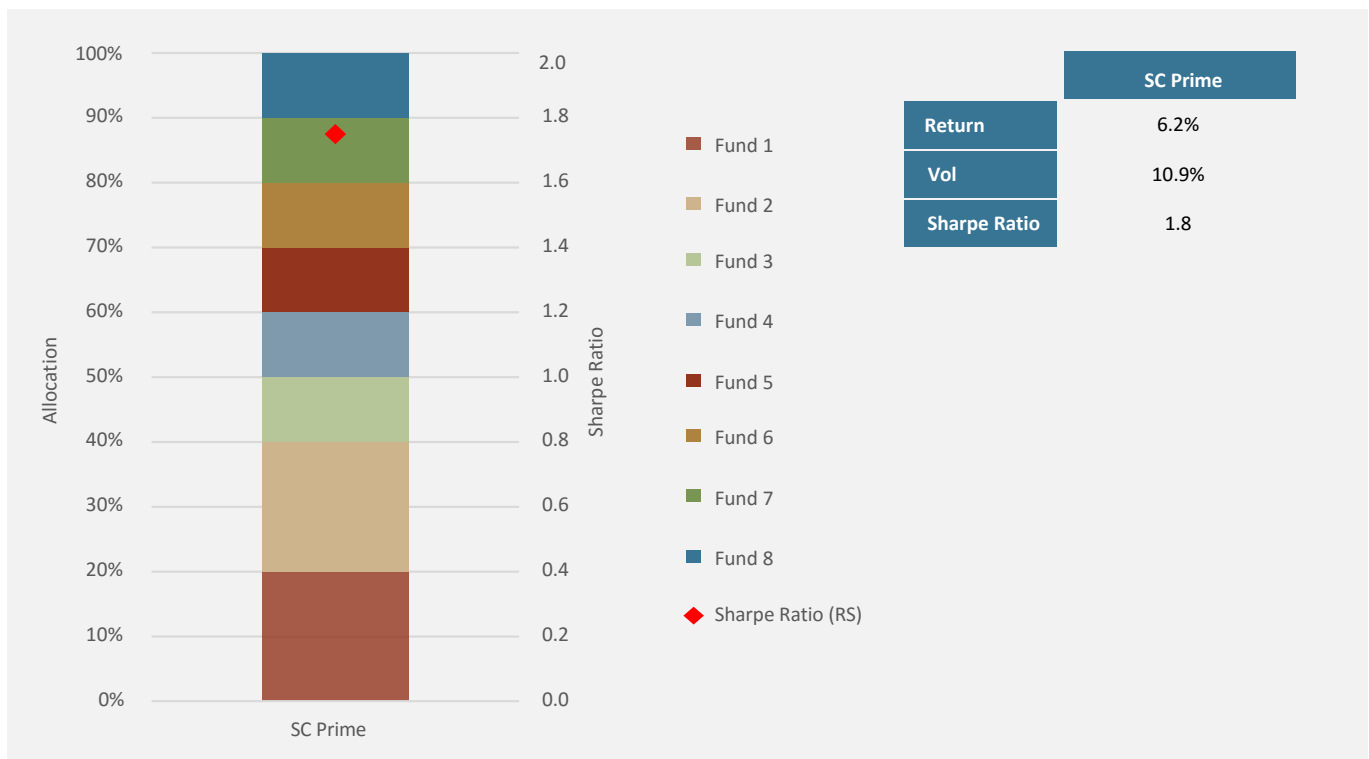
After analyzing the 5 scenarios, Minimum Volatility and Maximum Sharpe Ratio were ruled out as it is highly unlikely that one would significantly overweight one fund. While Minimum Volatility with Constraint was interesting, Maximum Sharpe Ratio with Constraint compared more favorably with a higher Sharpe Ratio and annualized return with minimal increase in annualized volatility. Although Equal Weight had the lowest Sharpe Ratio of the scenarios, it was also the most “intellectually honest” as overfitting can easily occur when using historical data. In other words, if we were to rely solely on optimizing based on risk and return, it may make sense to equal weight the funds as it is difficult to predict future risk and return. However, as noted above, there are a number of other factors to consider. By equal weighting funds, we would be placing little to no emphasis on manager experience and investment strategy, which is one of the dangers of the optimization process.



As both Equal Weight and Maximum Sharpe Ratio with Constraint were attractive, a simple conclusion may be to average the allocations resulting from these scenarios, which resulted in the following:

	Average	Equal Weight	Max Sharpe Ratio w/ Constraint
Return	10.8%	10.2%	11.7%
Vol	5.5%	6.0%	5.3%
Sharpe Ratio	1.9	1.7	2.1

This portfolio was composed of 2 larger fund allocations with the remainder balanced across the other 6 funds. Using this as a starting point, we hypothetically assigned 2 allocations a weight of 20% each and 6 a weight of 10% each. Fund 1 was assigned a larger allocation relative to the other scenarios given the manager’s track record and experience managing its strategy. Although Fund 4 was attractive on a volatility and Sharpe Ratio basis, its historical returns are at the lower end of the spectrum relative to peers. However, given its correlation and risk characteristics, Fund 4 can provide the portfolio strong diversification benefits. The remaining allocations were relatively in line with the average of Equal Weight and Maximum Sharpe Ratio with Constraints with adjustments made based on the factors discussed above. While this is a hypothetical portfolio, the combination of quantitative and qualitative methodologies is essential to Silver Creek’s portfolio construction framework.



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